

Practice with Examples

For use with pages 154–159

GOAL

Collect variables on one side of an equation and use equations to solve real-life problems

VOCABULARYAn **identity** is a linear equation that is true for all values of the variable.**EXAMPLE 1****Collecting Variables on One Side**Solve $20 - 3x = 2x$.**SOLUTION**Think of $20 - 3x$ as $20 + (-3x)$. Since $2x$ is greater than $-3x$, collect the x -terms on the right side.

$$20 - 3x = 2x$$

Write original equation.

$$20 - 3x + 3x = 2x + 3x$$

Add $3x$ to each side.

$$20 = 5x$$

Simplify.

$$\frac{20}{5} = \frac{5x}{5}$$

Divide each side by 5.

$$4 = x$$

Simplify.

Exercises for Example 1

Solve the equation.

1. $5q = -7q + 6$

2. $14d - 6 = 17d$

3. $-y + 7 = -8y$

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EXAMPLE 2 Many Solutions or No Solution

a. Solve $2x + 3 = 2x + 4$.

b. Solve $-(t + 5) = -t - 5$

SOLUTION

a. $2x + 3 = 2x + 4$

Write original equation.

$$2x + 3 - 3 = 2x + 4 - 3$$

Subtract 3 from each side.

$$2x = 2x + 1$$

Simplify.

$$0 = 1$$

Subtract $2x$ from each side.

The original equation has no solution, because $0 \neq 1$ for any value of x .

b. $-(t + 5) = -t - 5$

Write original equation.

$$-t - 5 = -t - 5$$

Use distributive property.

$$-5 = -5$$

Add t to each side.

All values of t are solutions, because $-5 = -5$ is always true.

The original equation is an *identity*.

Exercises for Example 2

Solve the equation.

4. $9z - 3 = 9z$

5. $2(f - 7) = 2f - 14$

6. $n + 3 = -5n$

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EXAMPLE 3 Solving Real-Life Problems

A health club charges nonmembers \$2 per day to swim and \$5 per day for aerobics classes. Members pay a yearly fee of \$200 plus \$3 per day for aerobics classes. Write and solve an equation to find the number of days you must use the club to justify a yearly membership.

SOLUTION

Let n represent the number of days that you use the club. Then find the number of times for which the two plans would cost the same.

$$2n + 5n = 200 + 3n \quad \text{Write real-life equation.}$$

$$7n = 200 + 3n \quad \text{Combine like terms.}$$

$$7n - 3n = 200 + 3n - 3n \quad \text{Subtract } 3n \text{ from each side.}$$

$$4n = 200 \quad \text{Simplify.}$$

$$\frac{4n}{4} = \frac{200}{4} \quad \text{Divide each side by 4.}$$

$$n = 50 \quad \text{Simplify.}$$

You must use the club 50 days to justify a yearly membership.

Exercises for Example 3

7. Rework Example 3 if nonmembers pay \$3 per day to swim.

8. Rework Example 3 if members pay a yearly fee of \$220.